

$$p_n(x) = \sum_{k=0}^n \frac{f^{(k)}(x_0)}{k!} (x - x_0)^k \quad p_n(x) = \sum_{i=0}^n y_i L_i(x) \quad L_i(x) = \prod_{\substack{k=0 \\ k \neq i}}^n \frac{(x - x_k)}{(x_i - x_k)}$$

$$d_k = \frac{c_{k+1} - c_k}{3h_k}$$

$$a_k + b_k h_k + c_k h_k^2 + d_k h_k^3 = a_{k+1}$$

$$f[x_k, x_{k+1}, \dots, x_{k+i}] = \frac{f[x_{k+1}, x_{k+2}, \dots, x_{k+i}] - f[x_k, x_{k+1}, \dots, x_{k+i-1}]}{x_{k+i} - x_k}$$

$$b_k + 2c_k h_k + 3d_k h_k^2 = b_{k+1} \quad X^{(n+1)} = G(X^{(n)}) \quad x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$A = \begin{bmatrix} 1 & 0 & 0 & 0 & \dots & 0 \\ h_0 & 2(h_0 + h_1) & h_1 & 0 & \dots & 0 \\ 0 & & \ddots & & & \vdots \\ \vdots & & & \ddots & & \vdots \\ 0 & \dots & 0 & h_{n-2} & 2(h_{n-2} + h_{n-1}) & h_{n-1} \\ 0 & \dots & 0 & 0 & 0 & 1 \end{bmatrix} \quad X = \begin{bmatrix} c_0 \\ c_1 \\ \vdots \\ c_{n-1} \\ c_n \end{bmatrix}$$

$$B = \begin{bmatrix} 0 \\ \frac{3}{h_1}(a_2 - a_1) - \frac{3}{h_0}(a_1 - a_0) \\ \vdots \\ \frac{3}{h_{n-1}}(a_n - a_{n-1}) - \frac{3}{h_{n-2}}(a_{n-1} - a_{n-2}) \\ 0 \end{bmatrix}$$

$$E_T = h^4 \frac{b-a}{180} f^{(iv)}(\xi)$$

$$x_{n+1} = g(x_n)$$

$$E = \frac{|X - \underline{X}|}{|X|}$$

$$A = \begin{bmatrix} 2h_0 & h_0 & 0 & 0 & \dots & 0 \\ h_0 & 2(h_0 + h_1) & h_1 & 0 & \dots & 0 \\ 0 & & \ddots & & & \vdots \\ \vdots & & & \ddots & & \vdots \\ 0 & \dots & 0 & h_{n-2} & 2(h_{n-2} + h_{n-1}) & h_{n-1} \\ 0 & \dots & 0 & 0 & h_{n-1} & 2h_{n-1} \end{bmatrix}$$

$$n \geq \frac{\log(b-a) - \log \varepsilon}{\log 2}$$

$$Y_{k+1} = Y_k + hf(t_k, Y_k)$$

$$x'(t_j) = \frac{x(t_j) - x(t_{j-1})}{h}$$

$$|E_T| = h^2 \frac{b-a}{12} |f''(\xi_k(x))| \quad E_T = -h^4 \frac{b-a}{80} f^{(iv)}(\xi) \quad \sigma^2 = \frac{\sum_{k=0}^n (p_m(x_k) - y_k)^2}{N - m - 1}$$

$$\int_a^b f(x) dx \approx \frac{h}{2} \left[f(a) + f(b) + 2 \sum_{k=1}^{n-1} f(x_k) \right] \quad d_3 = d_1 + \frac{x(b) - x(b)^{(1)}}{x(b)^{(2)} - x(b)^{(1)}} (d_2 - d_1)$$

$$\frac{\|\hat{X} - X\|}{\|X\|} \leq \frac{Cond(A)}{1 - Cond(A)} \frac{\|\delta A\|}{\|A\|} \left(\frac{\|\delta A\|}{\|A\|} + \frac{\|\delta b\|}{\|b\|} \right) \quad x'(t_j) = \frac{x(t_{j+1}) - x(t_{j-1})}{2h}$$

$$x_{n+1} = x_n - \frac{f(x_n)(x_n - x_{n-1})}{f(x_n) - f(x_{n-1})} \quad X^{(n+1)} = -D^{-1}(L + U)X^{(n)} + D^{-1}b$$

$$X^{(n+1)} = (D + L)^{-1}(-U)X^{(n)} + (D + L)^{-1}b$$

$$B = \begin{bmatrix} \frac{3}{h_0}(a_1 - a_0) - 3f'(x_0) \\ \frac{3}{h_1}(a_2 - a_1) - \frac{3}{h_0}(a_1 - a_0) \\ \vdots \\ \frac{3}{h_{n-1}}(a_n - a_{n-1}) - \frac{3}{h_{n-2}}(a_{n-1} - a_{n-2}) \\ 3f'(x_n) - \frac{3}{h_{n-1}}(a_n - a_{n-1}) \end{bmatrix}$$

$$c = \frac{a f(b) - b f(a)}{f(b) - f(a)}$$

$$c = \frac{a + b}{2}$$

$$E = |X - \underline{X}|$$

$$\sum_{i=0}^m \left(a_i \sum_{k=0}^n x_k^{i+j} \right) = \sum_{k=0}^n x_k^j y_k \quad \int_a^b f(x) dx \approx \frac{16(S(a, c) + S(c, b)) - S(a, b)}{15}$$

$$\int_a^b f(x) dx \approx \frac{3h}{8} \left[f(a) + f(b) + 3 \sum_{k=0}^{\frac{n-3}{3}} f(x_{3k+1}) + 3 \sum_{k=0}^{\frac{n-3}{3}} f(x_{3k+2}) + 2 \sum_{k=1}^{\frac{n-3}{3}} f(x_{3k}) \right]$$

$$x'(t_j) = \frac{x(t_{j+1}) - x(t_j)}{h} \quad R_{k,1} = \frac{1}{2} \left\{ R_{k-1,1} + h_{k-1} \sum_{i=1}^{2^{k-2}} f \left(a + \frac{2i-1}{2} h_{k-1} \right) \right\}$$

$$R_{i,j} = \frac{4^{j-1} R_{i,j-1} - R_{i-1,j-1}}{4^{j-1} - 1} \quad Y_{k+1} = Y_k + h Y_k' + \frac{h^2}{2} Y_k'' + \dots$$

$$\int_a^b f(x) dx \approx \frac{h}{3} \left[f(a) + f(b) + 4 \sum_{k=0}^{\frac{n-2}{2}} f(x_{2k+1}) + 2 \sum_{k=1}^{\frac{n-2}{2}} f(x_{2k}) \right]$$

$$Y_{k+1} = Y_k + \frac{1}{6} (K_1 + 2K_2 + 2K_3 + K_4) \quad \text{con} \quad \begin{cases} K_1 = h f(t_k, Y_k) \\ K_2 = h f \left(t_k + \frac{1}{2}h, Y_k + \frac{1}{2}K_1 \right) \\ K_3 = h f \left(t_k + \frac{1}{2}h, Y_k + \frac{1}{2}K_2 \right) \\ K_4 = h f(t_k + h, Y_k + K_3) \end{cases}$$

$$Y_{k+1} = Y_k + \frac{h}{2} [f(t_k, Y_k) + f(t_{k+1}, Y_k + h f(t_k, Y_k))] \quad E = \sqrt{\frac{\sum_{k=0}^n (p_m(x_k) - y_k)^2}{N}}$$

$$x''(t_j) = \frac{x(t_{j+1}) - 2x(t_j) + x(t_{j-1}))}{h^2} \quad E = \sum_{k=0}^n (p_m(x_k) - y_k)^2$$

$$E(x) \approx \left| \frac{(x - x_0)(x - x_1) \dots (x - x_n)}{(n+1)!} f^{(n+1)}(\xi(x)) \right|$$

$$E(x) \approx f[x_0, x_1, \dots, x_n, x](x - x_0)(x - x_1) \dots (x - x_n)$$